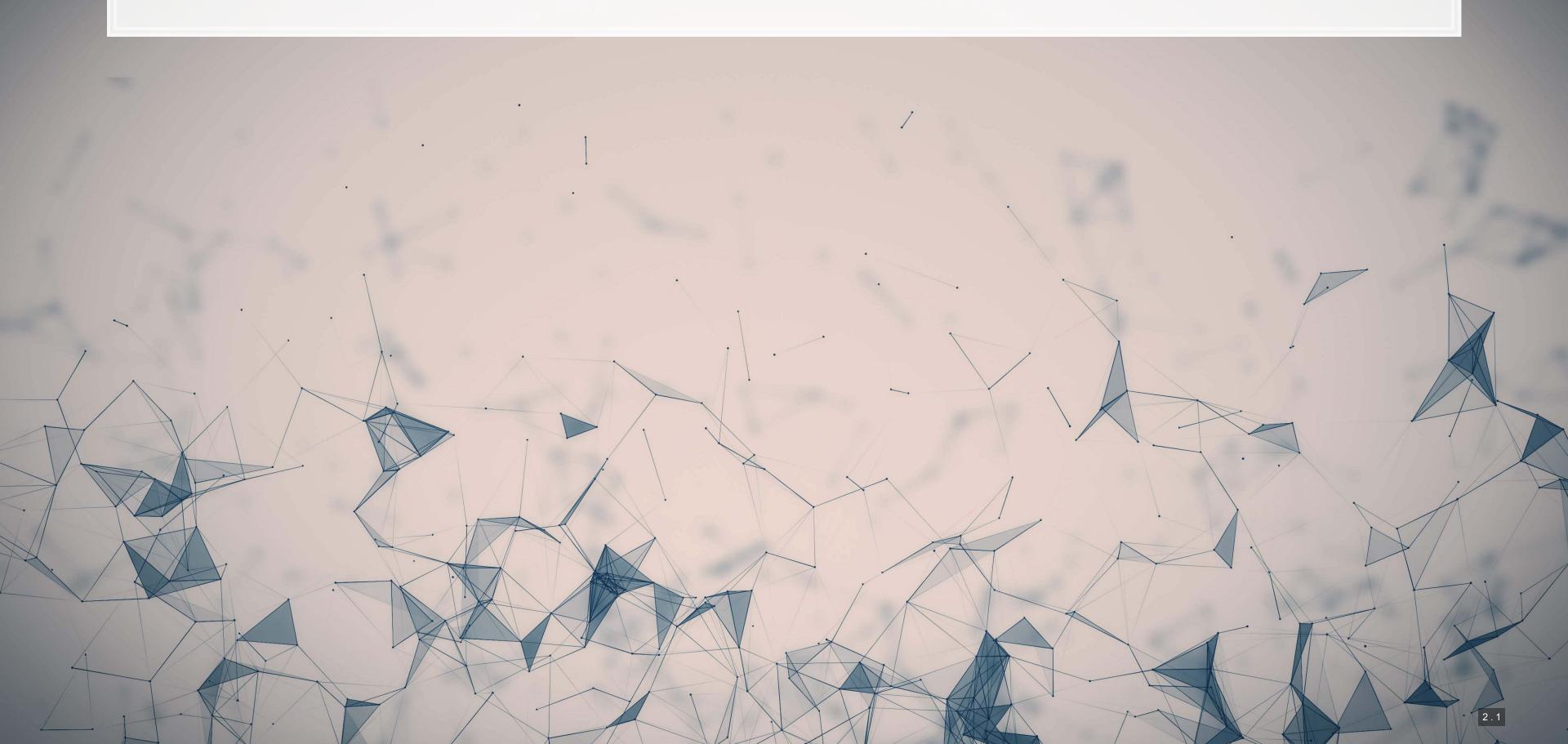
# ACCT 420: Logistic Regression

# Session 4

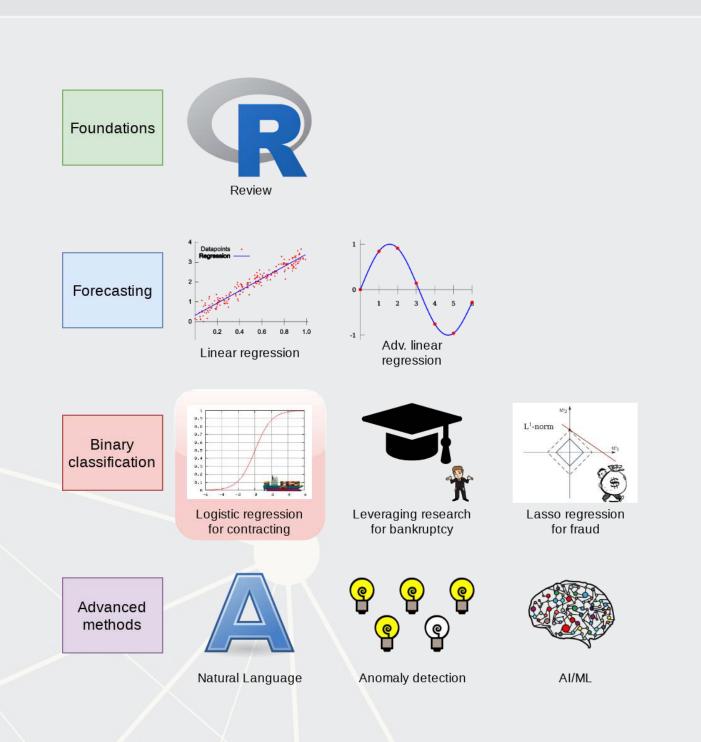
Dr. Richard M. Crowley

rcrowley@smu.edu.sg http://rmc.link/

#### **Front matter**



## Learning objectives



- Theory:
  - Understanding binary problems
- Application:
  - Detecting shipping delays caused by typhoons
- Methodology:
  - Logistic regression
  - Spatial visualization

## Datacamp

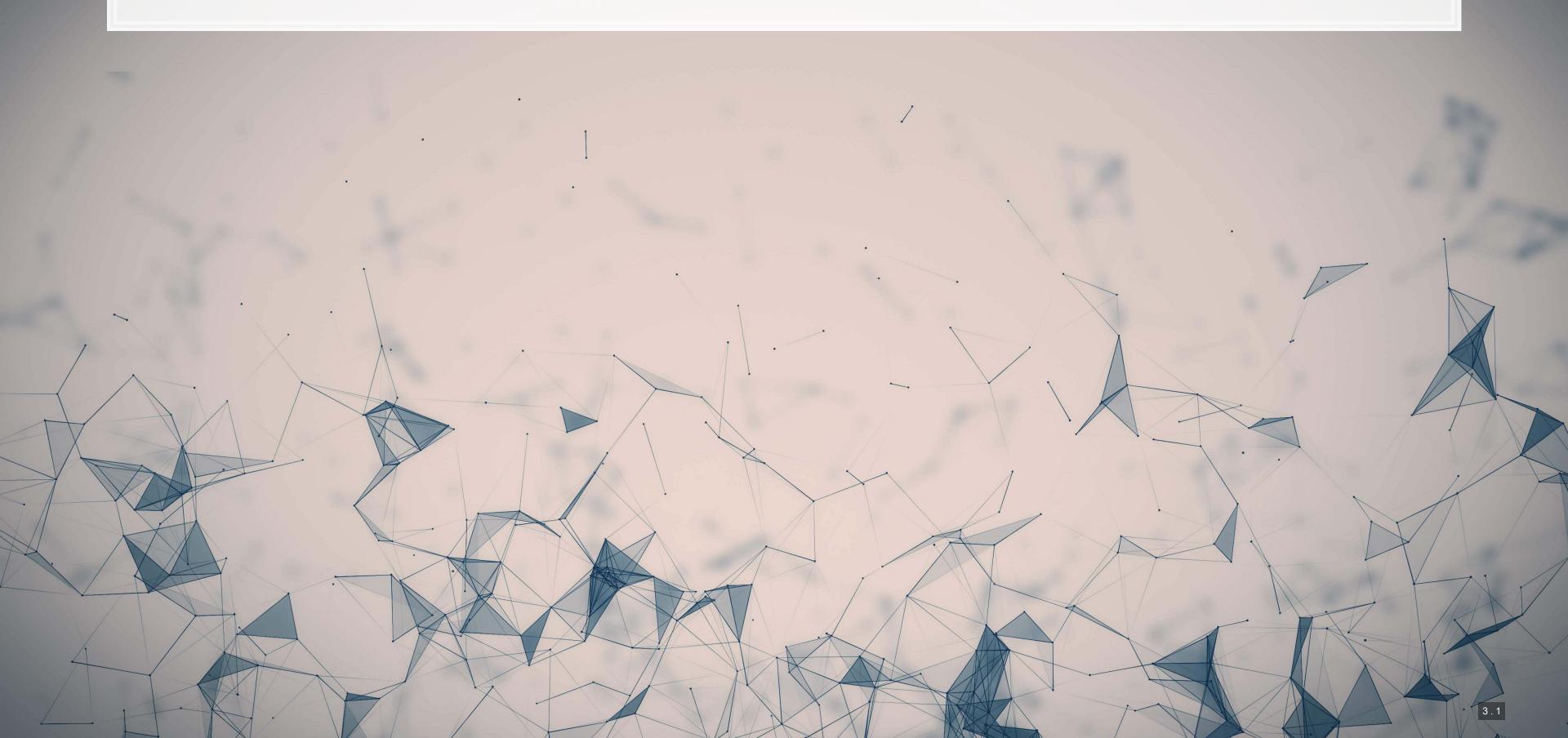
- Explore on your own
- No specific required class this week

#### **Assignment 2**

- Looking at Singaporean retail firms
  - Mostly focused on time and cyclicality
  - Some visualization
  - A little of what we cover today
- Optional (but encouraged):
  - You can work in pairs on this assignment
    - If you choose to do this, please only make 1 submission and include both your names on the submission



#### **Binary outcomes**



#### What are binary outcomes?

- Thus far we have talked about events with continuous outcomes
  - Revenue: Some positive number
  - Earnings: Some number
  - ROA: Some percentage
- Binary outcomes only have two possible outcomes
  - Did something happen, *yes* or *no*?
  - Is a statement *true* or *false*?

#### Accounting examples of binary outcomes

- Financial accounting:
  - Will the company's earnings meet analysts' expectations?
  - Will the company have positive earnings?
- Managerial accounting:
  - Will we have \_\_\_\_ problem with our supply chain?
  - Will our customer go bankrupt?
- Audit:
  - Is the company committing fraud?
- Taxation:
  - Is the company too aggressive in their tax positions?

We can assign a probability to any of these

# Brainstorming...

What types of business problems or outcomes are binary?



#### Regression approach: Logistic regression

- When modeling a binary outcome, we use logistic regression
  - A.k.a. logit model
- The *logit* function is  $logit(x) = log(\frac{x}{1-x})$ 
  - Also called log odds

$$\log\left(rac{ ext{Prob}(y=1|X)}{1- ext{Prob}(y=1|X)}
ight)=lpha+eta_1x_1+eta_2x_2+\ldots+arepsilon$$

There are other ways to model this though, such as probit

#### Implementation: Logistic regression

The logistic model is related to our previous linear models as such:

Both linear and logit models are under the class of General Linear Models (GLMs)

- To regress a GLM, we use the glm() command.
  - In fact, the lm() command we have been using is actually glm() when you specify the option family=gaussian
- To run a logit regression:

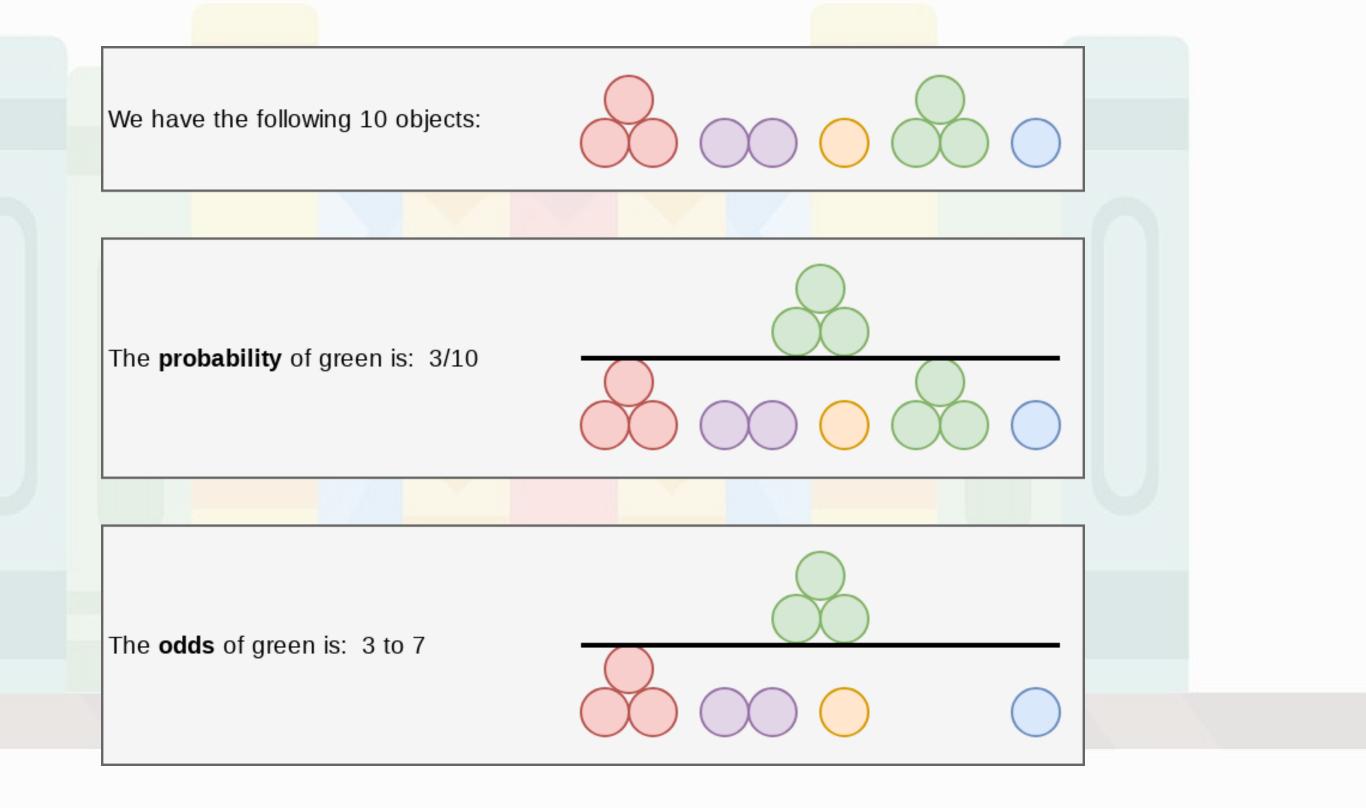
```
mod <- glm(y ~ x1 + x2 + x3 + ..., data=df, family=binomial)
summary(mod)</pre>
```

family=binomial is what sets the model to be a logit

#### Interpreting logit values

- The sign of the coefficients means the same as before
  - +: increases the likelihood of y occurring
  - -: decreases the likelihood of y occurring
- The level of a coefficient is different
  - The relationship isn't linear between  $x_i$  and y now
  - Instead, coefficients are in log odds
    - Thus,  $e^{\beta_i}$  gives you the odds, o
- You can interpret the odds for a coefficient
  - Increased by [o-1]%
- You need to sum all relevant log odds before converting to a probability!

# Odds vs probability



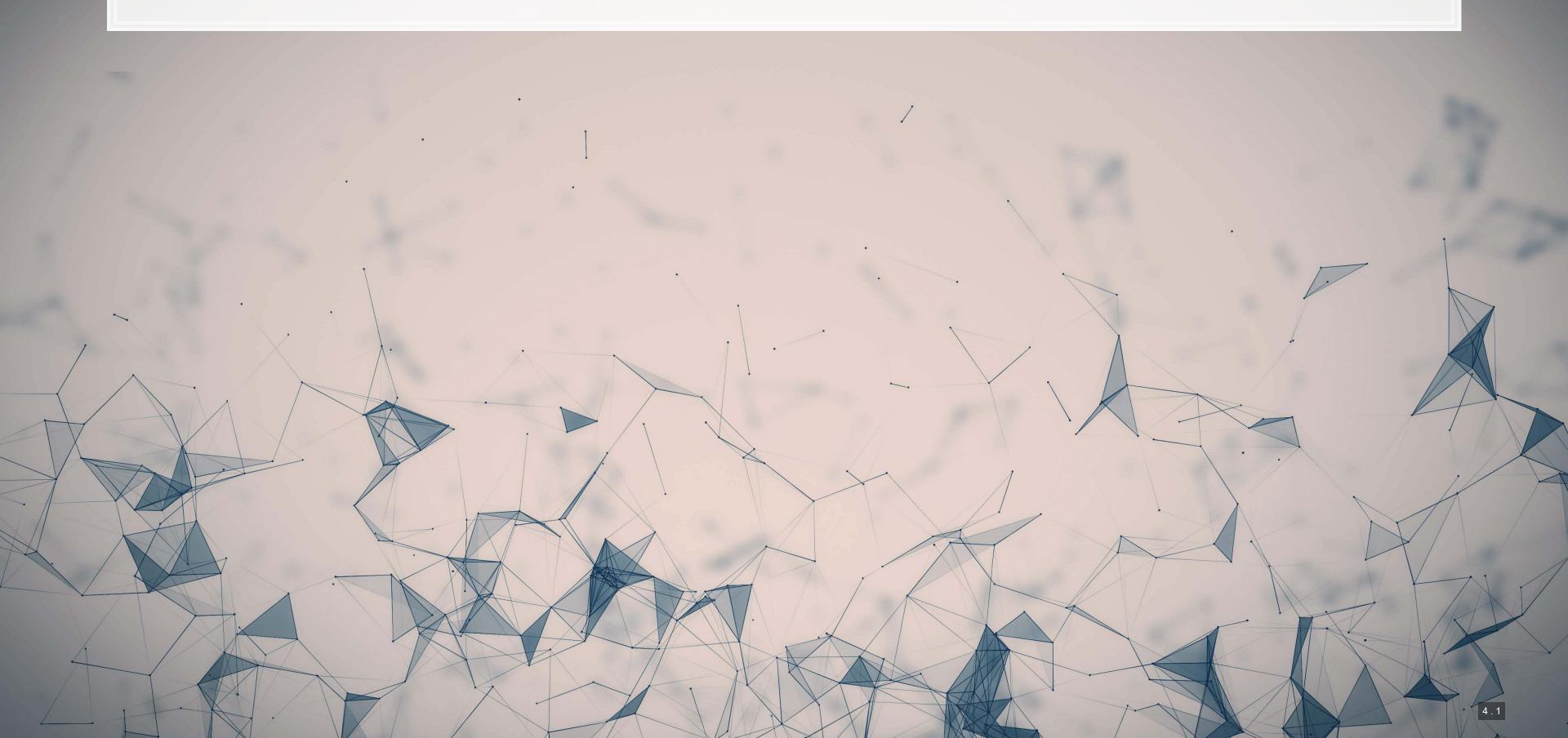
#### **Example logit regression**

Do holidays increase the likelihood that a department more than doubles its store's average weekly sales across departments?

```
# Create the binary variable from Walmart sales data
df$double <- ifelse(df$Weekly_Sales > df$store_avg*2,1,0)
fit <- glm(double ~ IsHoliday, data=df, family=binomial)
tidy(fit)</pre>
```

Holidays increase the odds... but by how much?

#### Logistic regression interpretation



#### A simple interpretation

• The model we just saw the following model:

 $logodds(Double\ sales) = -3.45 + 0.54 Is Holiday$ 

- There are two ways to interpret this:
  - 1. Coefficient by coefficient
  - 2. In total

#### Interpretting specific coefficients

$$logodds(Double\ sales) = -3.45 + 0.54 Is Holiday$$

- Interpreting specific coefficients is easiest done manually
- Odds for the IsHoliday coefficient are exp (0.54) = 1.72
  - This means that having a holiday modifies the baseline (i.e., non-Holiday) odds by 1.72 to 1
    - Where 1 to 1 is considered no change
  - Baseline is 0.032 to 1

```
# Automating the above:
exp(coef(fit))
```

## (Intercept) IsHolidayTRUE ## 0.03184725 1.71367497

#### Interpretting in total

- It is important to note that log odds are additive
  - So, calculate a new log odd by plugging in values for variables and adding it all up
    - Holiday: -3.45 + 0.54 \* 1 = -2.89
    - No holiday: -3.45 + 0.54 \* 0 = -3.45
- Then calculate odds and log odds like before
  - With holiday: exp(-2.89) = 0.056
  - Without holiday: exp(-3.45) = 0.032
  - Ratio of holiday to without: 1.72!
    - This is the individual log odds for holiday

We need to specify values to calculate log odds in total

#### Converting to probabilities

We can calculate a probability at any given point using the log odds

$$Probability = rac{odds}{odds + 1}$$

- Probability of double sales...
  - With a holiday: 0.056 / (0.056 + 1) = 0.052
  - Without a holiday: 0.032 / (0.032 + 1) = 0.031

These are easier to interpret, but require specifying values for each model input to calculate

### Using predict() to simplify it

- predict () can calculate log odds and probabilities for us with minimal effort
  - Specify type="response" to get probabilities

```
test_data <- as.data.frame(IsHoliday = c(0,1))
predict(model, test_data) # log odds

## [1] -3.44 -2.90

predict(model, test_data, type="response") #probabilities

## [1] 0.03106848 0.05215356
```

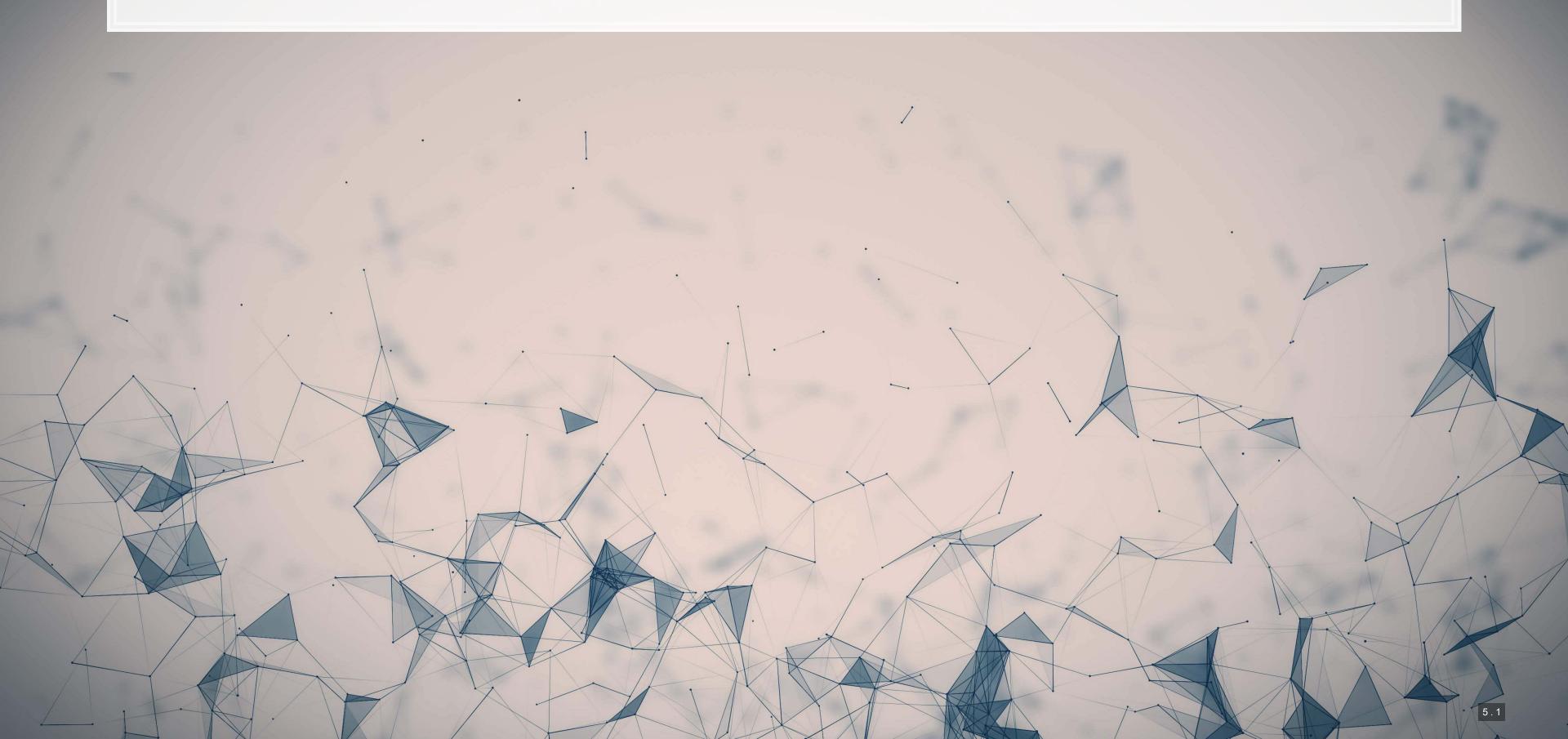
- Here, we see the baseline probability is 3.1%
- The probability of doubling sales on a holiday is higher, at 5.2%

#### R practice: Logit

- A continuation of last week's practices answering:
  - Is Walmart more likely to see a year over year decrease in quarterly revenue during a recession?
- Practice using mutate() and glm()
- Do exercises 1 and 2 in today's practice file
  - R Practice
  - Shortlink: rmc.link/420r4



#### Logistic regression interpretation redux



#### What about more complex models?

- Continuous inputs in the model
  - What values do we pick to determine probabilities?
- Multiple inputs?
  - We can scale up what we did, but things get messy
    - Mathematically, the inputs get interacted within the inner workings of logit...
      - So the impact of each input depends on the values of the others!

#### Consider this model

```
model2 <- glm(double ~ IsHoliday + Temperature + Fuel_Price, data=df, family=binomial)
summary(model2)</pre>
```

```
R
```

#### Odds and probabilities

```
# Odds
exp(coef(model2))
     (Intercept) IsHolidayTRUE
                                  Temperature
                                                  Fuel Price
                                                  0.7\overline{3}40376
       0.1692308
                                    0.9892316
                      1.4483570
# Typical September days
hday sep <- mean(predict(model2, filter(df, IsHoliday, month==9), type="response"))
no hday sep <- mean(predict(model2, filter(df, !IsHoliday, month==9), type="response"))
# Typical December days
hday dec <- mean(predict(model2, filter(df, IsHoliday, month==12), type="response"))</pre>
no hday dec <- mean(predict(model2, filter(df, !IsHoliday, month==12), type="response"))</pre>
html_df(data.frame(Month=c(9,9,12,12),
                   IsHoliday=c(FALSE, TRUE, FALSE, TRUE),
                   Probability=c(no_hday_sep, hday_sep, no_hday_dec, hday_dec)))
```

Month	IsHoliday	Probability			
9	FALSE	0.0266789			
9	TRUE	0.0374761			
12	FALSE	0.0398377			
12	TRUE	0.0586483			

#### A bit easier: Marginal effects

Marginal effects tell us the *average* change in our output for a change of 1 to an input

- The above definition is very similar to how we interpret linear regression coefficients
  - The only difference is the word *average* the effect changes a bit depending on the input data
- Using margins, we can calculate marginal effects
- There are a few types that we could calculate:
  - An Average Marginal Effect tells us what the average effect of an input is across all values in our data
    - This is the default method in the package
  - We can also specify a specific value to calculate marginal effects at (like with our probabilities last slides)

#### Marginal effects in action

```
# Calculate AME marginal effects
library(margins)
m <- margins(model2)
m</pre>
```

```
## Temperature Fuel_Price IsHoliday
## -0.0003377 -0.009644 0.01334
```

- A holiday increase the probability of doubling by a flat 1.33%
  - Not too bad when you consider that the probability of doubling is 3.23%
- If the temperature goes up by 1°F (0.55°C), the probability of doubling changes by -0.03%
- If the fuel price increases by 1 USD for 1 gallon of gas, the probability of doubling changes by -0.96%

#### margins niceties

We can get some extra information about our marginal effects through summary ():

```
summary(m) %>%
  html_df()
```



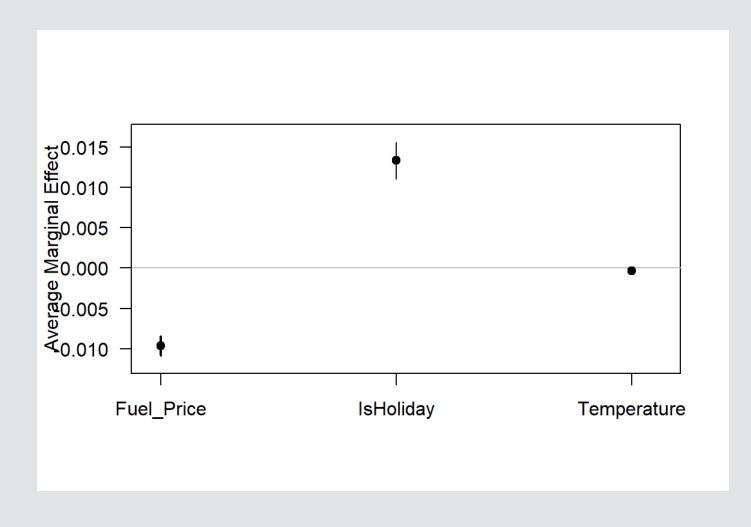
factor	AME	SE	Z	р	lower	upper
Fuel_Price	-0.0096438	0.0006163	-15.64800	0	-0.0108517	-0.0084359
IsHoliday	0.0133450	0.0011754	11.35372	0	0.0110413	0.0156487
Temperature	-0.0003377	0.0000149	-22.71255	0	-0.0003668	-0.0003085

- Those p-values work just like with our linear models
- We also get a confidence interval
  - Which we can plot!

# Plotting marginal effects

plot(m, which=summary(m) \$factor)





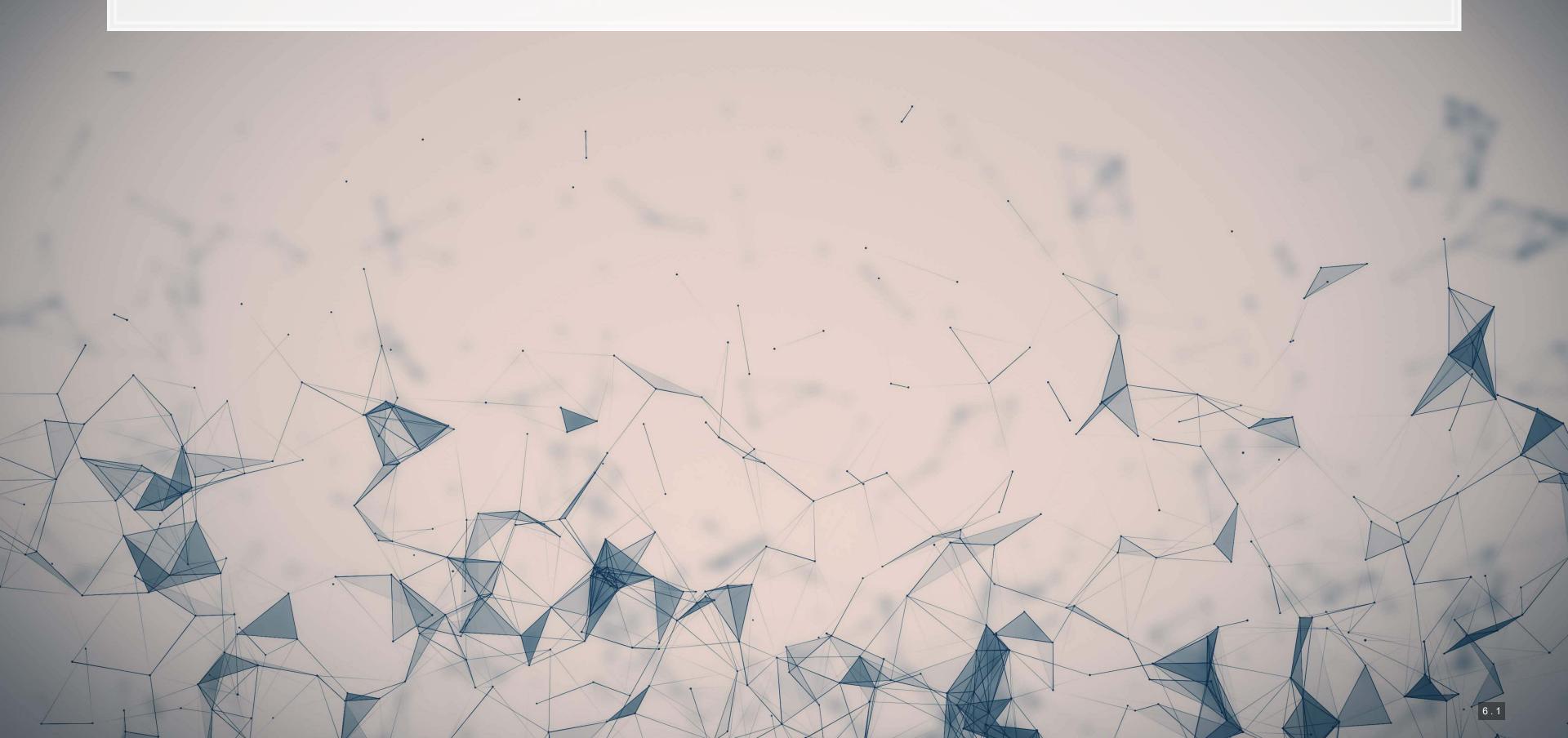
Note: The which... part is absolutely necessary at the moment due to a bug in the package

#### Marginal effects at a specified value

factor	IsHoliday	AME	SE	Z	р	lower	upper
Fuel_Price	FALSE	-0.0093401	0.0005989	-15.59617	0	-0.0105139	-0.0081664
Fuel_Price	TRUE	-0.0131335	0.0008717	-15.06650	0	-0.0148420	-0.0114250
Temperature	FALSE	-0.0003271	0.0000146	-22.46024	0	-0.0003556	-0.0002985
Temperature	TRUE	-0.0004599	0.0000210	-21.92927	0	-0.0005010	-0.0004188

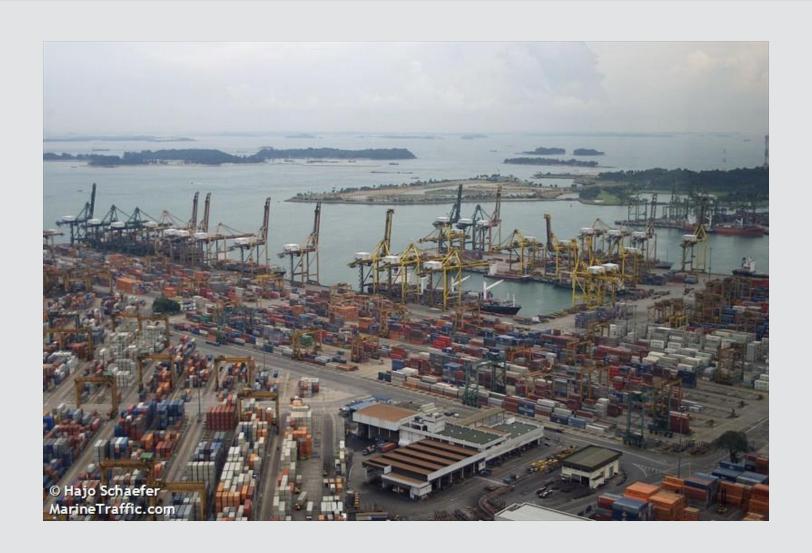
factor	Temperature	AME	SE	Z	р	lower	upper
IsHoliday	0	0.0234484	0.0020168	11.62643	0	0.0194955	0.0274012
IsHoliday	25	0.0184956	0.0015949	11.59704	0	0.0153697	0.0216214
IsHoliday	50	0.0144798	0.0012679	11.42060	0	0.0119948	0.0169648
IsHoliday	75	0.0112693	0.0010161	11.09035	0	0.0092777	0.0132609
IsHoliday	100	0.0087305	0.0008213	10.62977	0	0.0071207	0.0103402

## Today's Application: Shipping delays



# The question

Can we leverage global weather data to predict shipping delays?



#### **Formalization**

- 1. Question
  - How can predict naval shipping delays?
- 2. Hypothesis (just the alternative ones)
  - 1. Global weather data helps to predict shipping delays
- 3. Prediction
  - Use Logistic regression and z-tests for coefficients
  - No hold out sample this week too little data

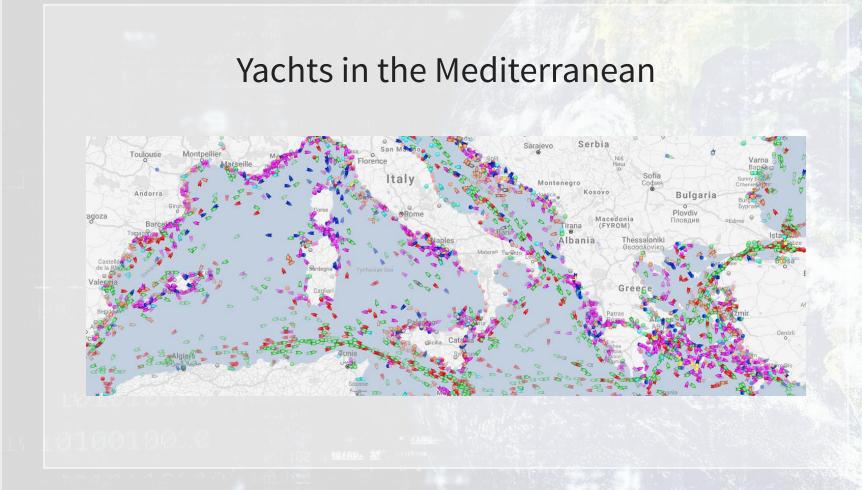
#### A bit about shipping data

- WRDS doesn't have shipping data
- There are, however, vendors for shipping data, such as:



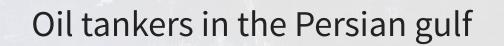
- They pretty much have any data you could need:
  - Over 650,000 ships tracked using ground and satellite based AIS
    - AIS: Automatic Identification System
  - Live mapping
  - Weather data
  - Fleet tracking
  - Port congestion
  - Inmarsat support for ship operators

#### What can we see from naval data?



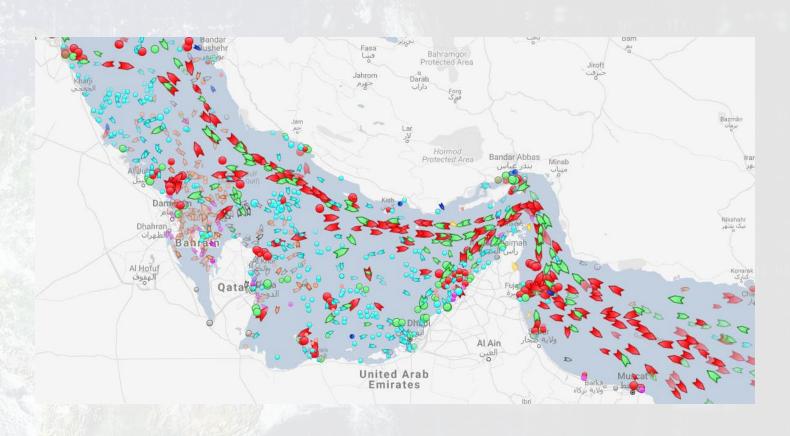
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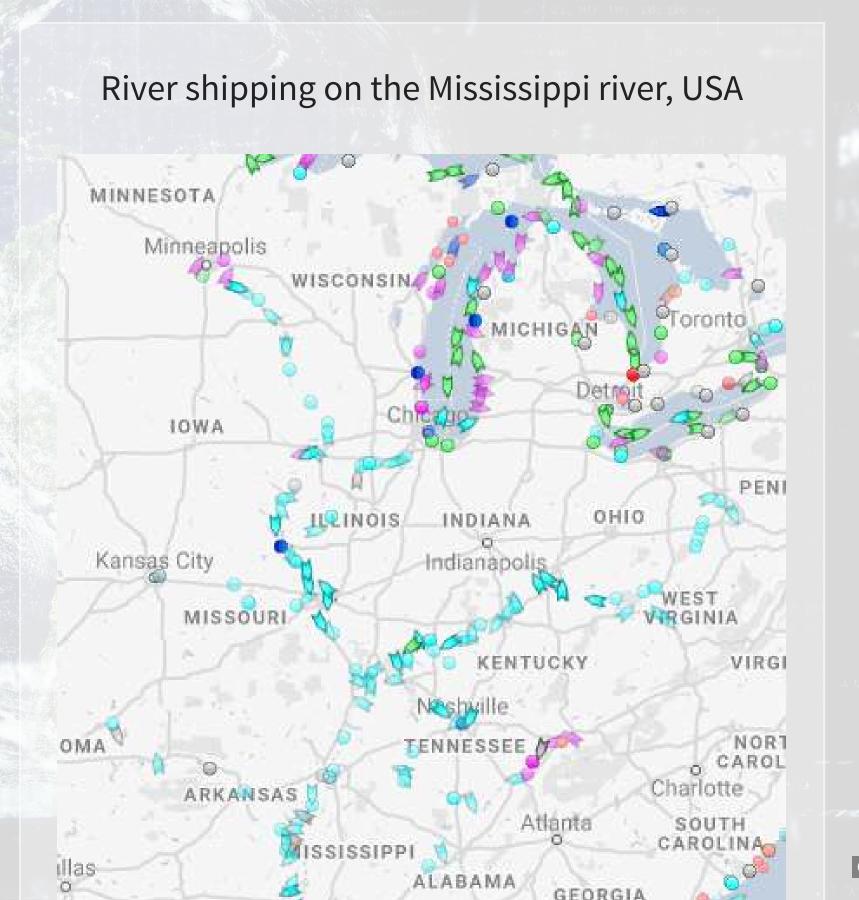


#### What can we see from naval data?



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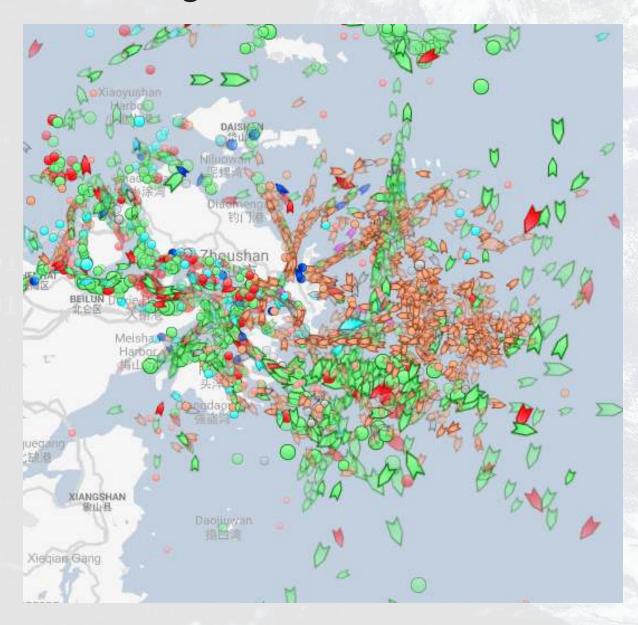


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(2)(2)(2)(4)

#### What can we see from naval data?

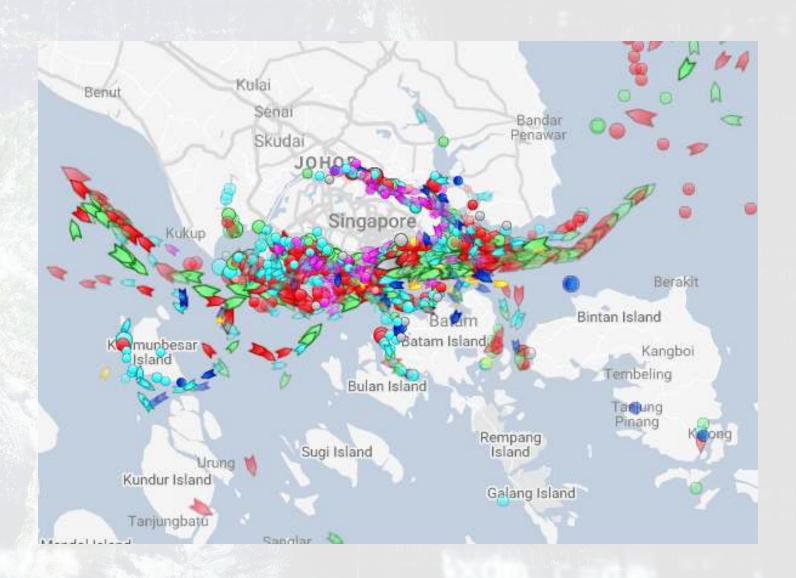
Busiest ports by containers and tons (Shanghai & Ningbo-Zhoushan, China)



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Busiest port for transshipment (Singapore)



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# Examining Singaporean owned ships Singaporean owned container and tanker ships, August 31, 2018 Port Cargo Tanker TYPHOON

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#### Code for last slide's map

- plot geo() is from plotly
- add markers () adds points to the map
- layout () adjusts the layout

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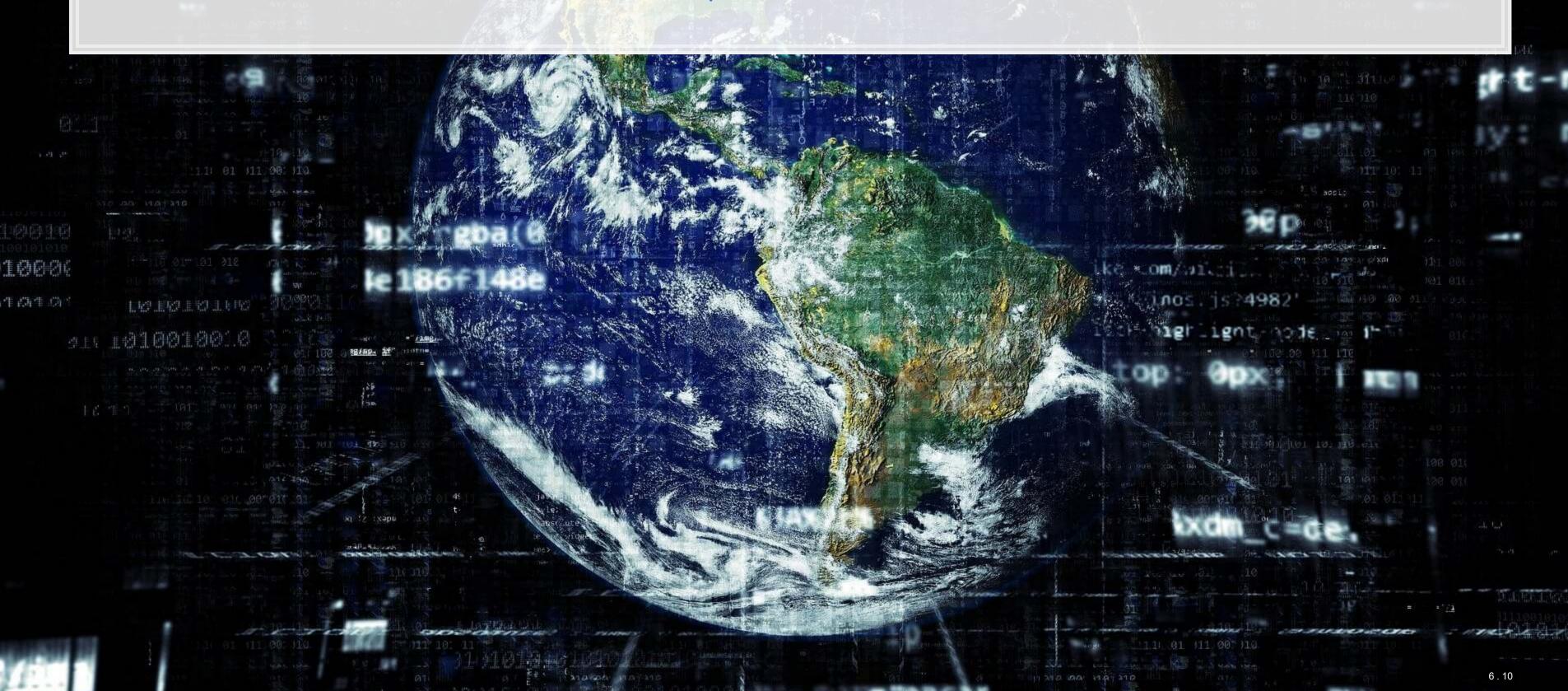
- Within geo, a list, the following makes the map a globe
  - projection=list(type="orthographic")

#### Singaporean ship movement

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(OCHE)

Link to ship movement animation



#### Code for last slide's map

world1 contains the map data

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- geom\_sf() plots map data passed to ggplot()
- geom\_point() plots ship locations as longitude and latitude
- ggplotly() converts the graph to html and animates it
  - Animation follows the frame aesthetic

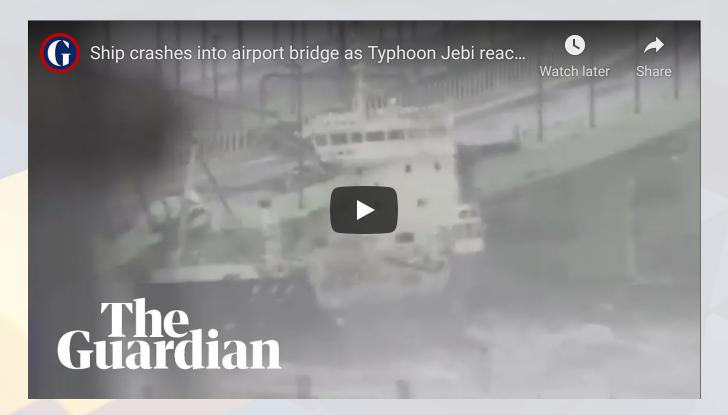
0

R

### What might matter for shipping? {data-background="../Backgrounds/group.jpg" class="default present-not"}+

What observable events or data might provide insight as to whether a naval shipment will be delayed or not?

#### **Typhoon Jebi**



- link
- Nullschool plot

## .0011000 (age) Typhoons in the data Singaporean container/tanker ships, September 4, 2018, evening • Typhoon Jebi 1000 1010

#### Code for last slide's map

This map is made the same way as the first map



#### Typhoons in the data using leaflet



#### Code for last slide's map

```
R
library(leaflet)
library(leaflet.extras)
# typhoon icons
icons <- pulseIcons(color='red',</pre>
 heartbeat = ifelse(typhoon Jebi$intensity vmax > 150/1.852, 0.8,
   ifelse(typhoon$intensity vmax < 118/1.852, 1.6, 1.2)),
 iconSize=ifelse(typhoon Jebi$intensity vmax > 150/1.852, 5,
   ifelse(typhoon Jebi$intensity vmax < 118/1.852, 2, 3)))
# ship icons
shipicons <- iconList(</pre>
 ship = makeIcon("../Figures/ship.png", NULL, 18, 18)
leaflet() %>%
 addTiles() %>%
 setView(lng = 136, lat = 34, zoom=4) %>%
 addPulseMarkers(data=typhoon Jebi[seq(1,nrow(typhoon Jebi),5),], lng=~lon,
                  lat=~lat, label=~date, icon=icons) %>%
 addCircleMarkers(data=typhoon Jebi[typhoon Jebi$intensity vmax > 150/1.852,],
```

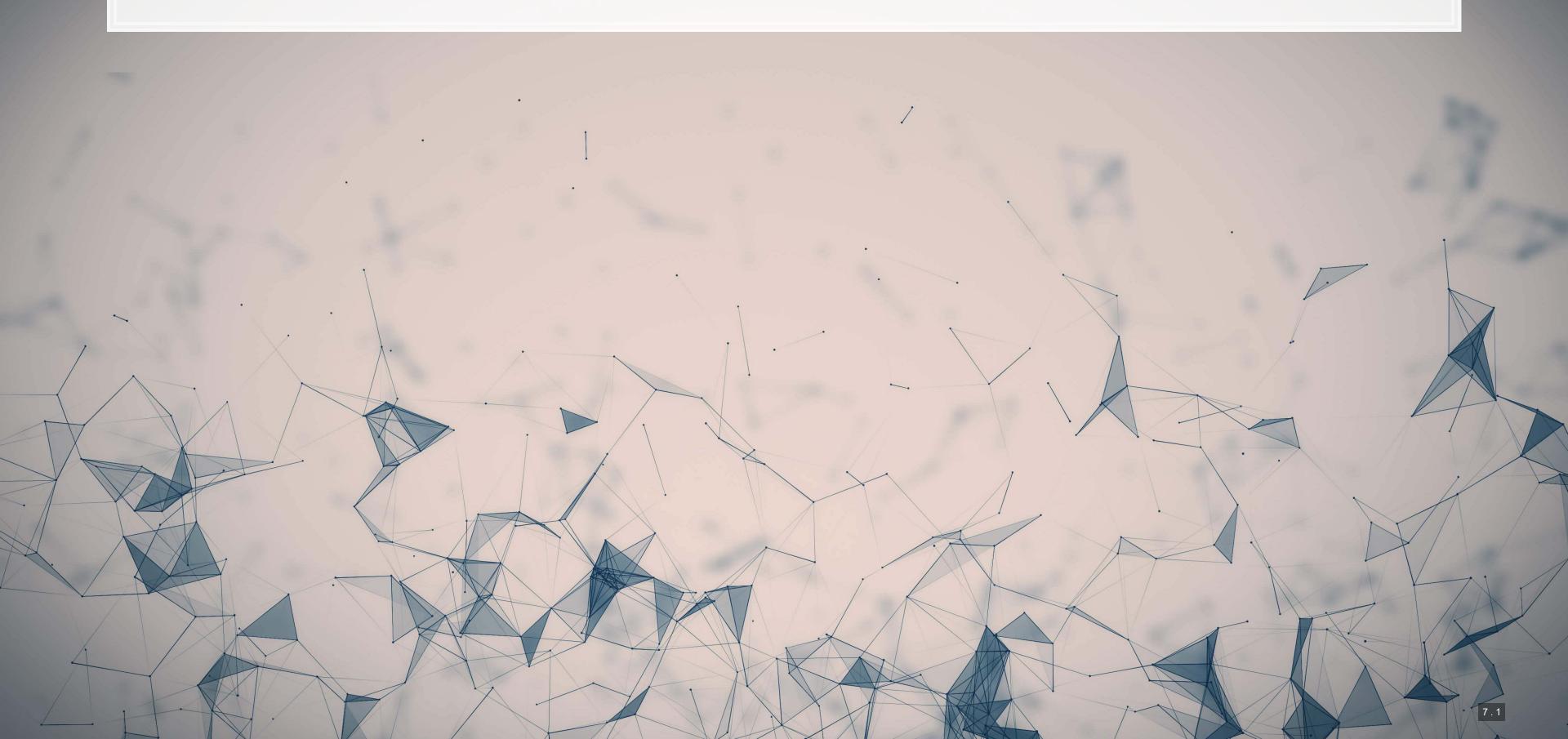
- pulseIcons(): pulsing icons from leaflet.extras
- iconList(): pulls icons stored on your computer
- leaflet():start the map; addTiles() pulls from OpenStreetMap
- setView(): sets the frame for the map
- addPulseMarkers(): adds pulsing markers
- addCircleMarkers():adds circular markers

#### R Practice on mapping

- Practice mapping typhoon data
  - 1 map using plotly
  - 1 map using leaflet
- Practice using plotly and leaflet
  - No practice using ggplot2 as sf is missing on DataCamp light
    - And sf can be tough to install for anyone on a Mac
- Do exercises 3 and 4 in today's practice file
  - R Practice
  - Shortlink: rmc.link/420r4



#### Predicting delays due to typhoons





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- If the ship will report a delay of at least 3 hours some time in the next 12-24 hours
- What we have:

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- Ship location
- Typhoon location
- Typhoon wind speed

We need to calculate distance between ships and typhoons

#### Distance for geo

- There are a number of formulas for this
  - Haversine for a simple calculation
  - Vincenty's formulae for a complex, incredibly accurate calculation
    - Accurate within 0.5mm
- Use distVincentyEllipsoid() from geosphere to get a reasonably quick and accurate calculation
  - Calculates distance between two sets of points, x and y, structured as matrices
  - Matrices must have longitude in the first column and latitude in the second column
  - Provides distance in meters by default

```
library(geosphere)
x <- as.matrix(df3[,c("lon","lat")]) # ship location
y <- as.matrix(df3[,c("ty_lon","ty_lat")]) # typhoon location

df3$dist_typhoon <- distVincentyEllipsoid(x, y) / 1000</pre>
```

#### Clean up

Some indicators to cleanly capture how far away the typhoon is

#### Do typhoons delay shipments?

```
## Call:
## glm(formula = delayed ~ typhoon 500 + typhoon 1000 + typhoon 2000,
      family = binomial, data = df3)
  Deviance Residuals:
                1Q Median
  -0.2502 \quad -0.2261 \quad -0.2261 \quad -0.2261 \quad 2.7127
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -3.65377
                          0.02934 - 124.547
                                              <2e-16 ***
## typhoon 500
               0.14073
                          0.16311
                                       0.863
                                              0.3883
## typhoon 1000 0.20539
                            0.12575
                                       1.633
                                               0.1024
## typhoon 2000 0.16059
                           0.07106
                                       2.260
                                              0.0238 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
  (Dispersion parameter for binomial family taken to be 1)
      Null deviance: 14329 on 59184 degrees of freedom
```

It appears so!

R

#### Interpretation of coefficients

```
odds1 <- exp(coef(fit1))
odds1

## (Intercept) typhoon_500 typhoon_1000 typhoon_2000
## 0.02589334 1.15111673 1.22800815 1.17420736</pre>
```

Ships 1,000 to 2,000 km from a typhoon have a 17% increased odds of having a delay

```
m1 <- margins(fit1)
summary(m1)

## factor AME SE z p lower upper
## typhoon_1000 0.0052 0.0032 1.6322 0.1026 -0.0010 0.0115
## typhoon_2000 0.0041 0.0018 2.2570 0.0240 0.0005 0.0076
## typhoon_500 0.0036 0.0042 0.8626 0.3883 -0.0046 0.0117
```

• Ships 1,000 to 2,000 km from a typhoon have an extra 0.41% chance of having a delay (baseline of 2.61%)

#### What about typhoon intensity?

- Hong Kong's typhoon classification: Official source
  - 1. 41-62 km/h: Tropical depression
  - 2. 63-87 km/h: Tropical storm
  - 3. 88-117 km/h: Severe tropical storm
  - 4. 118-149 km/h: **Typhoon**
  - 5. 150-184 km/h: Severe typhoon
  - 6. 185+km/h: Super typhoon

```
##
## (-1,41] (41,62] (62,87] (87,117] (117,149] (149,999]
## 3398 12039 12615 11527 2255 21141
```

#### Typhoon intensity and delays

```
A tibble: 10 x 5
                         estimate std.error statistic p.value
   term
                                      <dbl>
   <chr>
                            <dbl>
                                                <dbl> <dbl>
 1 (Intercept)
                                     0.0290 -126.
                         -3.65
 2 typhoon 500:Weak
                         -0.00879
                                     0.213
                                              -0.0413 0.967
 3 typhoon 500:Moderate
                        0.715
                                     0.251
                                                    0.00430
 4 typhoon 500:Super
                         -8.91
                                   123.
                                              -0.0726 0.942
 5 typhoon 1000:Weak
                          0.250
                                     0.161
                                                      0.121
 6 typhoon 1000:Moderate 0.123
                                     0.273
                                               0.451 0.652
 7 typhoon 1000:Super
                         -0.0269
                                     0.414
                                              -0.0648 0.948
 8 typhoon 2000:Weak
                          0.182
                                     0.101
                                               1.80
                                                    0.0723
 9 typhoon 2000: Moderate 0.0253
                                     0.134
                                               0.189 0.850
10 typhoon 2000:Super
                          0.311
                                     0.136
                                               2.29
                                                      0.0217
```

Moderate storms predict delays when within 500km

Super typhoons predict delays when 1,000 to 2,000km away

#### Interpretation of coefficients

m2 <- margins(fit2)
summary(m2) %>%
 html\_df()

factor	AME	SE	z	р	lower	upper
Moderate	0.0007378	0.0006713	1.0990530	0.2717449	-0.0005779	0.0020535
Super	-0.0050241	0.0860163	-0.0584087	0.9534231	-0.1736129	0.1635647
typhoon_1000	0.0035473	0.0036186	0.9802921	0.3269420	-0.0035450	0.0106396
typhoon_2000	0.0039224	0.0017841	2.1985908	0.0279070	0.0004257	0.0074191
typhoon_500	-0.0440484	0.6803640	-0.0647424	0.9483791	-1.3775373	1.2894405
Weak	0.0009975	0.0005154	1.9353011	0.0529534	-0.0000127	0.0020077

- Delays appear to be driven mostly by 2 factors:
  - 1. A typhoon 1,000 to 2,000 km away from the ship
  - 2. Weak typhoons

R

#### Interpretating interactions

factor	Weak	AME	SE	Z	р	lower	upper
typhoon_1000	1	0.0073057	0.0053682	1.360938	0.1735332	-0.0032157	0.0178271
typhoon_2000	1	0.0067051	0.0031225	2.147328	0.0317671	0.0005850	0.0128251
typhoon_500	1	-0.0458116	0.7052501	-0.064958	0.9482075	-1.4280764	1.3364531
factor	Moderate	AME	SE	Z	р	lower	upper
typhoon_1000	1	0.0059332	0.0078245	0.7582856	0.4482800	-0.0094025	0.0212688
typhoon_2000	1	0.0044871	0.0039453	1.1373050	0.2554108	-0.0032457	0.0122198
typhoon_500	1	-0.0311946	0.6847130	-0.0455586	0.9636620	-1.3732074	1.3108182
factor	Super	AME	SE	Z	р	lower	upper
typhoon_1000	1	0.0030638	0.0111295	0.2752891	0.7830941	-0.0187495	0.0248772
typhoon_2000	1	0.0102513	0.0041568	2.4661549	0.0136572	0.0021041	0.0183985
typhoon_500	1	-0.2241250	3.1608062	-0.0709076	0.9434713	-6.4191913	5.9709413

#### What might matter for shipping?

What other observable events or data might provide insight as to whether a naval shipment will be delayed or not?

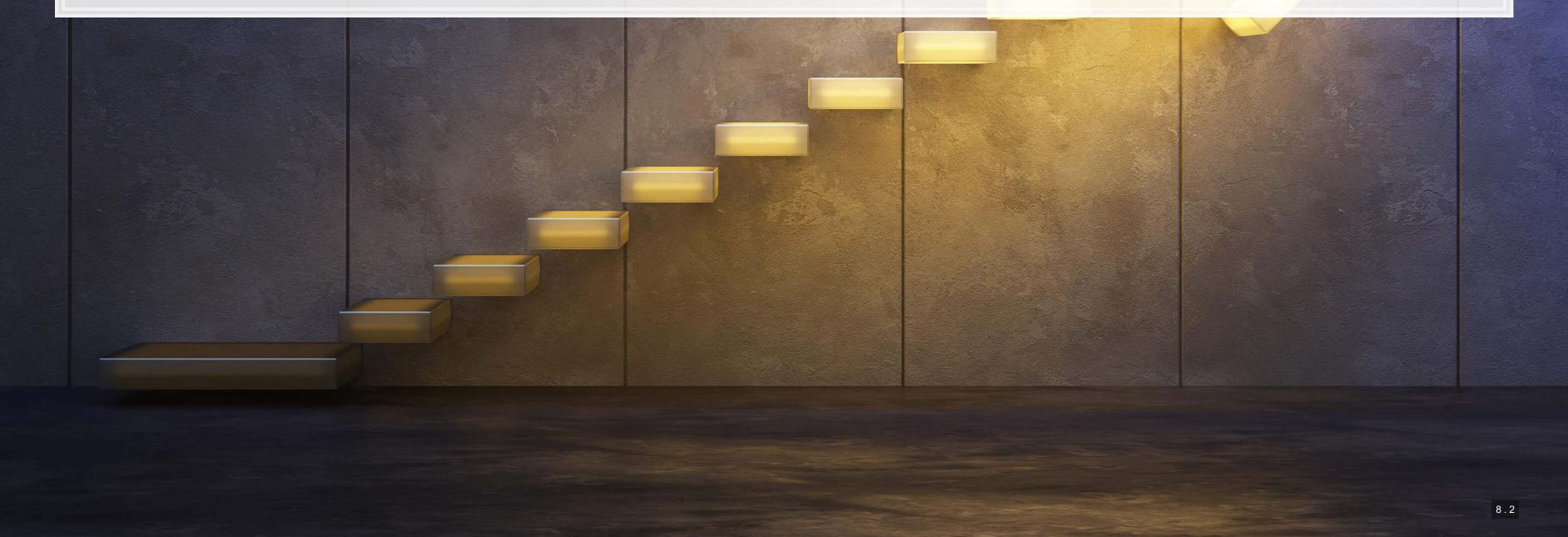
- What is the reason that this event or data would be useful in predicting delays?
  - I.e., how does it fit into your mental model?







- For next week:
  - Second individual assignment
    - Finish by 2 classes from now
    - Submit on eLearn
  - Think about who you want to work with for the project



#### Packages used for these slides

- broom
- geosphere
- kableExtra
- knitr
- leaflet
- leaflet.extras
- lubridate
- magrittr

- margins
- maps
- maptools
- plotly
- revealjs
- rgeos
- sf
- tidyverse

#### **Custom code**

```
# styling for plotly maps
geo <- list(</pre>
 showland = TRUE,
 showlakes = TRUE,
 showcountries = TRUE,
 showocean = TRUE,
 countrywidth = 0.5,
 landcolor = toRGB("grey90"),
 lakecolor = toRGB("aliceblue"),
 oceancolor = toRGB("aliceblue"),
 projection = list(
   type = 'orthographic', # detailed at https://plot.ly/r/reference/#layout-geo-projection
   rotation = list(
    lon = 100,
    lat = 1,
    roll = 0
 lonaxis = list(
   showgrid = TRUE,
   gridcolor = toRGB("gray40"),
   gridwidth = 0.5
 lataxis = list(
   showgrid = TRUE,
   gridcolor = toRGB("gray40"),
   gridwidth = 0.5
```